



$Y_p$ : RNA plasma,  $Y_D$ : RNA DBS,  $X$ : cons  
 $1 = \text{detected}, 0 = \text{not}$

sens:  $P(Y_D = 1 | Y_p = 1, X) = \gamma_1$  non-differential  
indep of  $X$ ,  $X$  and  $Y_p$

spec:  $P(Y_D = 0 | Y_p = 0, X) = 1 - \gamma_0$   $\gamma_0 = P(Y_D = 1 | Y_p = 0, X)$   
non-differential

Our model: logistic or RR model for  $X$  and  $Y_p$

$Y_p$  not observed but misclassification probs "known"  
for generalized linear model theory and Newhaus (1999)

②  $\mu_p(X) = P(Y_p = 1 | X)$  follows a GLM

$$g_p \{ \mu_p(X) \} = \eta_p = X\beta_p \quad Y_p \sim \text{binomial}$$

$g_p = \text{logit, logistic reg} ; g_p = \log, RR \text{ reg}$

Newhaus (99)  
Note:  $\mu(X) = P(Y_D = 1 | X) = \gamma_0 + (\gamma_1 - \gamma_0) \mu_p(X)$   
which is a GLM where link  $g$  is

$$g \{ \mu(X) \} = g_p \left\{ \frac{\mu_p(X) - \gamma_0}{(\gamma_1 - \gamma_0)} \right\} = \eta_p$$

$$\mu(X) = g_p^{-1} \{ \eta_p \} (\gamma_1 - \gamma_0) + \gamma_0$$

$g_p$ : logit for logistic  $g_p$ : log for RR

This is a GLM with a modified link function

Stata allows you to write these. I wrote one for ORs and one for RRs.

Need to calculate

$$\frac{\partial \mu}{\partial \eta} \quad \text{logit} \quad \log$$
$$(\gamma_1 - \gamma_0) \exp(\eta) (1 - \exp(\eta)) \quad (\gamma_1 - \gamma_0) e^\eta$$

$$\frac{\partial^2 \mu}{\partial \eta^2} \quad (\gamma_1 - \gamma_0) \frac{e^\eta (1 - e^\eta)}{(1 + e^\eta)^3} \quad (\gamma_1 - \gamma_0) e^\eta$$

These are programmed in two ado file

"mislogit" and "mislog"

sens spec  
From Ingrid :  $\gamma_1 = 0.808, 1 - \gamma_0 = 0.873$

$$\Rightarrow \gamma_0 = 0.127$$

$$\gamma_1 - \gamma_0 = 0.681$$

type "sysdir" in Stata. It tells you where "ado" files go. For me its

~ / Library / Application Support / stata / ado / personal

If you put the ado files there, the code works

```

program mislog
version 14.2
args todo eta mu return
if `todo' == -1 {
    /* Set global macros for output */
    global SGLM_Lt "misclassified log"
    global SGLM_If "log( (p-0.127)/0.681)"
    exit
}
if `todo' == 0 {
    /* set eta =g(mu) */
    generate double `eta' = log( (`mu' - 0.127)/0.681 )
    exit
}
if `todo' == 1 {
    /* set g^{-1}(eta) */
    generate double `mu' = exp(`eta')*0.681 + 0.127
    exit
}
if `todo' == 2 {
    /* set return = dmu/deta */
    local d2 = 0.681*exp(`eta')
    generate double `return' = 0.681*exp(`eta')
    exit
}
if `todo' == 3 {
    /* set return =d2mu/dmu2 */
    generate double `return' = 0.681*exp(`eta')
    exit
}
display as error "Unknown call to glm link function"
exit 198
end

```

```

program mislogit
version 14.2
args todo eta mu return
if `todo' == -1 {
    /* Set global macros for output */
    global SGLM_Lt "logit with missclassification"
    global SGLM_If "logit(((p - 0.127)/0.681))"
    exit
}

```

```

}

if `todo' == 0 {
    /* set eta =g(mu) */
    generate double `eta' = logit( (`mu' - 0.127)/0.681) )
    exit
}
if `todo' == 1 {
    /* set g^{-1}(eta) */
    generate double `mu' = (invlogit(`eta')*0.681) + 0.127
    exit
}
if `todo' == 2 {
    /* set return = dmu/deta */
    generate double `return' = 0.681*invlogit(`eta')*(1-invlogit(`eta'))
    exit
}
if `todo' == 3 {
    /* set return =d2mu/dmu2 */
    generate double `return' = 0.681*( exp(`eta')*(1-exp(`eta')) )/( (1+exp(`eta'))^3 )
    exit
}
display as error "Unknown call to glm link function"
exit 198
end

```